## Year 12 Maths - Pure and Statistics Teacher

| Topic |  | Ref | Ex |
| :---: | :---: | :---: | :---: |
| Algebraic Manipulation, Indices and Surds | Algebraic manipulation <br> - Multiply and divide integer powers. <br> - Expand single brackets and collect like terms. <br> - Expand the product of two or three expressions. <br> - Factorise linear, quadratic and cubic expressions. | P2.1 | $\begin{aligned} & \text { P1A } \\ & \text { P1B } \\ & \text { P1C } \end{aligned}$ |
|  | Indices <br> - Understand and be able to use the laws of indices <br> - Evaluate expressions including negative, fractional and zero indices <br> - Understand that fractional indices correspond to roots <br> - Powers of negative bases | P2.1 | P1D |
|  | Surds <br> - Be able to use and manipulate surds <br> - Multiplication and division <br> - Difference of squares <br> - Rationalise denominators of the forms $a \sqrt{ } b$ and ( $a+/-\sqrt{ } b$ ). | P2.2 | $\begin{aligned} & \text { P1E } \\ & \text { P1F } \end{aligned}$ |
| Further Algebra | Algebraic Division <br> - Cancel factors in algebraic fractions <br> - Divide a polynomial by a linear expression | P2.6 | $\begin{aligned} & \text { P7A } \\ & \text { P7B } \end{aligned}$ |
|  | Factor Theorem <br> - Know and be able to apply the factor theorem <br> - Use the factor theorem to fully factorise a cubic expression | P2.6 | P7C |
| Binomial Expansion | Proof <br> - Understand and be able to use the structure of mathematical proof, proceeding from given assumptions through a series of logical steps to a conclusion. <br> - Use the following methods of proof: <br> - Proof by deduction <br> - Proof by exhaustion <br> - Disproof by counter example | P1.1 | $\begin{aligned} & \text { P7D } \\ & \text { P7E } \end{aligned}$ |
|  | - Understand and be able to use the binomial expansion of $(a+b x)^{n}$ for positive integer $n$ <br> - Use Pascal's triangle or factorial notation for expansions <br> - Find an individual coefficient in a binomial expansion <br> - Use a binomial expansion to make approximations | P4.1 | $\begin{aligned} & \text { P8A } \\ & \text { P8B } \\ & \text { P8C } \\ & \text { P8D } \end{aligned}$ |
| Assessment 1 |  |  |  |

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| :---: | :---: | :---: | :---: |
| Probability | - Identify mutually exclusive events and use the addition rule. <br> - Identify independent events and use the multiplication rule. <br> - Make use of Venn diagrams and tree diagrams when solving probability problems. <br> - Link to discrete and continuous distributions probability represents area under a curve for continuous distribution. | A3. 1 | $\begin{aligned} & \text { P5A } \\ & \text { P5B } \\ & \text { P5C } \\ & \text { P5D } \end{aligned}$ |
| Statistical Distributions | Probability Distributions <br> - Understand and be able to use simple, discrete probability distributions (NO mean or variance) <br> - Know and be able to identify the discrete uniform distribution <br> - Calculate probabilities using the binomial distribution <br> - Use a calculator to find individual or cumulative binomial probabilities. | A4. 1 | $\begin{aligned} & \hline \text { P6A } \\ & \text { P6B } \\ & \text { P6C } \end{aligned}$ |
| Differentiation | Definition and differentiating polynomials <br> - Understand and be able to use the derivative of $f(x)$ as the gradient of the tangent to the graph of $y=\mathrm{f}(x)$ at a general point $(x, y)$ <br> - Interpret $\mathrm{dy} / \mathrm{dx}$ as the rate of change of y with respect to x . <br> - Differentiation from first principles for small positive integer powers of $x$ <br> - Sketch the gradient function for a given curve <br> - Differentiate $x^{\mathrm{n}}$, for rational values of n , and related constant multiples, sums and differences. Including those that require algebraic manipulation first. <br> - Understand and use the second derivative as the rate of change of gradient. | $\begin{aligned} & \text { P7.1 } \\ & \text { P7.2 } \end{aligned}$ | $\begin{gathered} \text { P12A } \\ \text { P12B } \\ \text { P12 } \\ \text { C } \\ \text { P12 } \\ \text { D } \\ \text { P12E } \end{gathered}$ |
|  | Applications of differentiation <br> - Use the derivative to solve problems involving gradients, tangents and normal. <br> - Identify increasing and decreasing functions <br> - Find stationary points of functions and determine their nature. | P7.3 | $\begin{gathered} \text { P12F } \\ \text { P12 } \\ \text { G } \\ \text { P12 } \\ \text { H } \\ \text { P121 } \\ \text { P12J } \end{gathered}$ |

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| Trigonometry | Trigonometric Ratios and Graphs <br> - Use the definitions of sine, cosine and tangent for all arguments <br> - Sketch the graphs of the sine, cosine and tangent functions <br> - Sketch simple transformations of these graphs | P5.2 | P9E P9F <br> P9G |
|  | Trigonometric Identities and Equations <br> - Know and use the relationships: $\tan x=\frac{\sin x}{\cos x} \text { and } \sin ^{2} x+\cos ^{2} x=1$ <br> - Solve trigonometric equations within a given interval including one of the form: <br> - $\sin \left(x+70^{\circ}\right)=0.5$ <br> - $3+5 \cos 2 x=1$ <br> - $6 \cos ^{2} x+\sin x-5=0$ <br> - Find multiple solutions in a given range using CAST diagram or graphs | $\begin{aligned} & \text { P5.3 } \\ & \text { P5.4 } \end{aligned}$ | P10A <br> P10B <br> P10C <br> P10D <br> P10E <br> P10F |
|  | Sine rule, cosine rules and $1 / 2 A B \sin C$ <br> - Be able to use the sine and cosine rules to find missing sides and angles <br> - Find the area of a triangle using $1 / 2 A B \sin C$ | P5.1 | $\begin{aligned} & \text { P9A } \\ & \text { P9B } \\ & \text { P9C } \\ & \text { P9D } \end{aligned}$ |
| Statistical <br> Sampling | Sampling Terminology <br> - Understand and be able to use the terms 'population' and 'sample' <br> - Use samples to make informal inferences about the population. <br> - Describe advantages and disadvantages of sampling compared to census. | A1.1 | A1A |
|  | Sampling Techniques <br> - Understand and be able to use sampling techniques <br> - Simple random sampling <br> - Stratified sampling <br> - Systematic sampling <br> - Quota sampling <br> - Opportunity (or convenience) sampling <br> - Describe advantages/disadvantages of techniques <br> - Select or critique sampling techniques in the context of solving a statistical problem; <br> - Understand that different samples can lead to different conclusions about the population. | A1.1 | A1A |

## Year 12 Maths - Pure and Statistics Teacher

| Topic |  | Ref | Ex |
| :---: | :---: | :---: | :---: |
| Data Presentation and Interpretation | Measures of location and variation <br> - Calculate measures of central tendency (location) mean, median and mode; <br> - Calculate measures of variation - standard deviation, variance, range and interpercentile range <br> - Use linear interpolation to calculate percentiles from grouped data. <br> - Be able to interpret and draw inferences from summary statistics. | A2.3 | A2A <br> A2B <br> A2C <br> A2D <br> A2E |
|  | Coding Understand and use coding for both mean and standard deviation calculations. | A2.3 | A2F |
| Data Presentation and Interpretation | Single Variable Data <br> - Interpret diagrams for single variable data: <br> - Histograms <br> - Frequency polygons <br> - Cumulative frequency diagrams <br> - Box and Whisker plots (including outliers) | A2. 1 | $\begin{aligned} & \text { A3A } \\ & \text { A3B } \\ & \text { A3C } \\ & \text { A3D } \end{aligned}$ |
|  | Bivariate Data <br> - Interpret scatter diagrams and regression lines for bivariate data <br> - Recognise the explanatory (independent) and response (dependent) variables <br> - Be able to make predictions using the regression line and understand its limitations (danger of extrapolation) <br> - Identify and interpret correlation, using terms 'positive', 'negative', 'zero', 'strong' and 'weak'. Understand that correlation does not imply causation | A2. 2 | $\begin{aligned} & \text { A4A } \\ & \text { A4B } \end{aligned}$ |
|  | Outliers and Cleaning Data <br> - Recognise and interpret possible outliers in data sets and statistical diagrams. (Any rule to be used will be specified in the question.) <br> - Select or critique data presentation techniques in the context of a statistical problem. <br> Clean data, including dealing with missing data, errors and outliers. | A2.4 | A3A |
| Assessment 3 |  |  |  |

## Year 12 Maths - Pure and Statistics Teacher

| Topic |  | Ref | Ex |
| :---: | :---: | :---: | :---: |
| Hypothesis testing | Principles and language of hypothesis testing <br> - Understand the language and concept of hypothesis testing, developed through a binomial model <br> - Understand that a sample is used to make an inference about a population <br> - Understand the terms: <br> - Null hypothesis $\mathrm{H}_{0}$ <br> - Alternative hypothesis $\mathrm{H}_{1}$ <br> - Critical value <br> - Critical region <br> - Significance level <br> - one-tail test <br> - two-tail test <br> - Acceptance region <br> - $p$-value | A5. 1 <br> A5. 2 | $\begin{aligned} & \text { P7A } \\ & \text { P7B } \end{aligned}$ |
|  | Conducting hypothesis testing <br> - Find critical values of a binomial distribution using tables or a calculator <br> - Appreciate that the significance level is the probability of incorrectly rejecting the null hypothesis <br> - Be able to calculate the critical region and the $p$-value <br> - Carry out a one-tailed or two-tailed test for the proportion of the binomial distribution and interpret the results in context. | $\begin{aligned} & \text { A5.1 } \\ & \text { A5.2 } \end{aligned}$ | $\begin{aligned} & \text { P7C } \\ & \text { P7D } \end{aligned}$ |
| Year 12 Pure Maths Mock |  |  |  |
| Functions | The modulus function \|| <br> - Understand and use the modulus function $\mathrm{y}=\|\mathrm{f}(\mathrm{x})\|$. <br> - Sketch graphs of modulus functions of the form $y=\|f(x)\|$ or $y=f(\|x\|)$. <br> - Use graphs to solve equations and inequalities involving the modulus function. | P2.7 | $\begin{aligned} & \text { P2A } \\ & \text { P2E } \end{aligned}$ |
|  | Function definition <br> - Understand mappings and functions <br> Use domain and range to define a function. | P2.8 | P2B |
|  | Composite Functions <br> - Combine two or more functions to make a composite function. <br> Find the domain and range for composite functions. | P2.8 | P2C |
|  | Inverse Functions <br> - Know how to find the inverse of a function both algebraically and graphically. <br> State the domain and range for an inverse function. | P2.8 | P2D |
|  | Combining Transformations <br> - Apply a combination of two (or more) transformations to the same curve. <br> Transform the modulus function \| |. | P2.9 | $\begin{aligned} & \hline \text { P2F } \\ & \text { P2G } \end{aligned}$ |

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| Topic |  | Ref | Ex |
| :---: | :---: | :---: | :---: |
| Start Year 13 Maths Course |  |  |  |
| Algebraic manipulation | Using Partial Fractions <br> - Review of simplifying algebraic fractions <br> - Use and apply models that involve quadratic functions, expressing as partial fractions | P4.1 | $\begin{gathered} 1 \mathrm{~B}, \mathrm{C} \\ \mathrm{D}, \mathrm{E}, \\ \mathrm{~F} \end{gathered}$ |
| Sequences and Series | Arithmetic Sequences <br> - Find the nth term of an arithmetic sequence. <br> - Understand the difference between a sequence and a series. <br> - Prove and use the formula for the sum of the first $n$ terms of an arithmetic series. | P4.4 | $\begin{aligned} & \text { P3A } \\ & \text { P3B } \end{aligned}$ |
|  | Geometric Sequences <br> - Find the nth term of a geometric sequence. <br> - Prove and use the formula for the sum of a finite geometric series. <br> Prove and use the formula for the sum to infinity of a convergent geometric series. | P4.5 | $\begin{aligned} & \text { P3C } \\ & \text { P3D } \\ & \text { P3E } \end{aligned}$ |
|  | Sigma notation Use and understand sigma $\sum$ notation to describe series | P4.3 | P3F |
|  | Recurrence Relations <br> - Generate sequences from recurrence relations of the form $u_{n+1}=F\left(u_{n}\right)$. <br> Be able to recognise increasing, decreasing and periodic sequences written as a recurrence relation. | P4.2 | $\begin{aligned} & \text { P3G } \\ & \text { P3H } \end{aligned}$ |
|  | Modelling with Series <br> Model real-life situations with sequences and series. | P4.6 | P31 |

